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## 4.1 Cubic graphs

1a.  $y = (x+1)(x-2)(x+3)$

x intercept set  $y = 0$

$x = -1 \quad x = 2 \quad x = -3$

y intercept set  $x = 0$

$y = (0+1)(0-2)(0+3)$

$y = -6$



2b.  $y = -x^3 - 2x^2 + 3x$

$x(1-x)(x+3)$

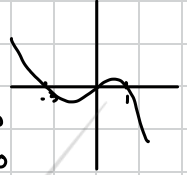
x intercept set  $y = 0$

$x = 0 \quad x = 1 \quad x = -3$

y intercept set  $x = 0$

$0(1-0)(0+3)$

$y = 0$



b.  $y = x(2x-1)(2x+1)$

x intercept set  $y = 0$

$x = 0 \quad x = 1/2 \quad x = -1/2$

y intercept set  $x = 0$

$y = 0(2(0)-1)(2(0)+1)$

$y = 0$



2c.  $y = 6x^3 - 3x^2$

$3x^2(2x-1)$

x intercept set  $y = 0$

$x = 0 \quad x = 1/2$

y intercept set  $x = 0$

$3(0)^2(2(0)-1)$

$y = 0$



c.  $y = (x-2)(x+4)(x+4)$

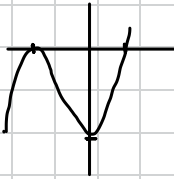
x intercept set  $y = 0$

$x = 2 \quad x = -4 \quad x = -4$

y intercept set  $x = 0$

$y = (0-2)(0+4)(0+4)$

$y = -32$



3a.  $y = (x-2)(x^2+x+3)$

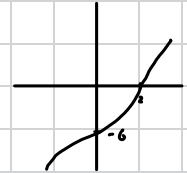
x intercept set  $y = 0$

$x = 2$

y intercept set  $x = 0$

$y = (0-2)(0^2+0+3)$

$y = -6$



2a.  $y = x^3 + 2x^2 + 3x$

$x(x-1)(x+3)$

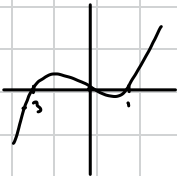
x intercept set  $y = 0$

$x = 0 \quad x = 1 \quad x = -3$

y intercept set  $x = 0$

$y = 0(0-1)(0+3)$

$y = 0$



3b.  $y = (x-3)^3$

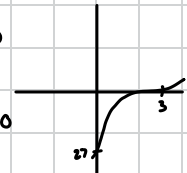
x intercept set  $y = 0$

$x = 3$

y intercept set  $x = 0$

$(0-3)^3$

$y = -27$



$$3c. y = -(x-4)^3$$

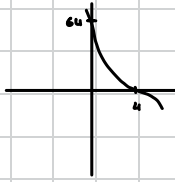
$$\underline{x \text{ intercept}} \quad \text{set } y = 0$$

$$x = 4$$

$$\underline{y \text{ intercept}} \quad \text{set } x = 0$$

$$y = -(0-4)^3$$

$$y = 64$$



$$4a. x^3 + 8x^2 + 16x$$

$$x(x+4)(x+4)$$

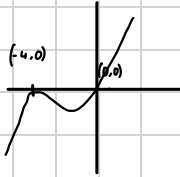
$$b. \underline{x \text{ intercept}} \quad \text{set } y = 0$$

$$x = 0 \quad x = -4 \quad x = -4$$

$$\underline{y \text{ intercept}} \quad \text{set } x = 0$$

$$0(0+4)(0+4)$$

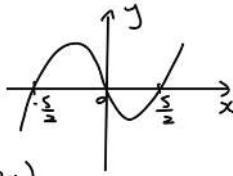
$$y = 0$$



$$5a. y = 25x - 4x^3$$

$$y = x(25 - 4x^2)$$

$$y = x(5-2x)(5+2x)$$



$$5b. \text{When } x = 0, y = 0$$

$$\text{When } y = 0, 0 = x(5-2x)(5+2x)$$

$$x = 0 \text{ or } \frac{5}{2} \text{ or } -\frac{5}{2}$$

$$6a. \text{assume the coefficient of } x^3 \text{ is 1}$$

$$6b. y = a(x+6)(x-6)^2$$

$$\text{Sub } (-2, 32)$$

$$32 = a(-2+6)(-2-6)^2$$

$$32 = a(4)(-8)^2$$

$$32 = 256a$$

$$a = \frac{1}{8}$$

$$7a. (x-1)^2(x-4)$$

$$(x-1)(x-1)(x-4)$$

$$(x^2 - x - x + 1)(x-4)$$

$$x^3 - 4x^2 - x^2 + 4x - x^2 + 4x + x - 4$$

$$x^3 - 6x^2 + 9x - 4$$

$$a = 1 \quad b = 6 \quad c = 9$$

$$b. \underline{y \text{ intercept}} \quad \text{set } x = 0$$

$$(0-1)^2(0-4)$$

$$y = -4 \quad (0, -4)$$

$$8. y = a(x+1)(x-2)(x-5)$$

$$\text{When } x = 0, y = 30$$

$$30 = a(1)(-2)(-5)$$

$$a = 3$$

$$y = 3(x+1)(x-2)(x-5)$$

$$y = 3(x^2 - x - 2)(x-5)$$

$$y = 3(x^3 - 6x^2 + 3x + 10)$$

$$y = \underline{\underline{3x^3 - 18x^2 + 9x + 30}}$$