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## 1.3: Hypothesis testing for zero correlation

① Given:  $n=30$ ,  $r=0.4125$

$H_0: \rho=0$ ;  $H_1: \rho>0$  → positive correlation

a) at the 5% level:  $0.05$ ;  $p=0.3061 < 0.4125$ . Reject  $H_0$ : there is reason to believe at the 5% level of significance that there is a correlation between the scores.

b) at the 1% level:  $0.01$ ;  $p=0.4226 > 0.4125$ . Accept  $H_0$ : there is no evidence of correlation between the two scores at the 1% level of significance.

② Given:  $n=12$ ,  $r=0.62$

$H_0: \rho=0$ ;  $H_1: \rho \neq 0$

a) 10% level: → Two-tailed test: significance level (0.05)

→  $p=0.4973 < 0.05$ ; Reject  $H_0$ : there is reason to believe at the 10% level of significance that there is a correlation between the mass and the length of the otters.

b) 2% level: → Two-tailed test: significance level (0.01)

→  $p=0.6581 > 0.01$ . Accept  $H_0$ : there is no evidence of correlation between the mass and the length of the otters at the 2% level of significance.

③ a)  $r = -0.728$  (3SF)

b)  $H_0: \rho=0$ ,  $H_1: \rho \neq 0$  (Two-tailed test: SL: 0.025)

→  $p=0.8114 > 0.025$ . Accept  $H_0$ : there is no evidence of correlation between the engine size and fuel economy at the 5% level of significance.

④ a)  $H_0: \rho=0$ ,  $H_1: \rho>0$  (positive correlation)

$p=0.7887 < 0.861$ . Reject  $H_0$ : there is evidence of linear correlation at the 1% level of significance. There is evidence to suggest the company is correct.

⑤ Given:  $r = -0.51$

$H_0: \rho=0$ ,  $H_1: \rho<0$  (Negative correlation)

→  $p=0.4116$ . Reject  $H_0$ : there is evidence of negative correlation at the 1% level of significance. There is evidence to suggest the council is correct.

⑥ Given:  $n=12$ ,  $r=0.7$

→ To reject the null hypothesis. Least possible would be 1% (as  $p=0.3981 < 0.7$ )

⑦ Given:  $r = -0.833$  Negative correlation:  $\rho < 0$  SL: 0.005

To find the sample possible sample size,  $p$  has to less than 0.833.

For  $n=9$ ,  $0.7977 < 0.833$ .

⑧ a)  $r = 0.812$

b)  $H_0: \rho = 0$ ,  $H_1: \rho > 0$  (One-tailed test as  $\rho > 0$ ; SL: 0.1)

$\Rightarrow p = 0.7887 < 0.812$ . Reject  $H_0$ : there is evidence of positive correlation at the 1% level of significance.

⑨ a)  $r = 0.786$

b)  $H_0: \rho = 0$ ,  $H_1: \rho > 0$  (One-tailed test as  $\rho > 0$ ; SL: 0.025)

$\Rightarrow p = 0.7067 < 0.786$ . Reject  $H_0$ : there is evidence of linear correlation at the 2.5% level of significance.

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