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1) a) $(3-x)^5$

$$1(3)^5(-x)^0 + 5(3)^4(-x)^1 + 10(3)^3(-x)^2 + 10(3)^2(-x)^3 + 5(3)^1(-x)^4 + 1(3)^0(-x)^5$$

$$243 - 405x + 270x^2 - 90x^3 + 15x^4 - x^5$$

b) $(2x+y)^4$

$$1(2x)^4(y)^0 + 4(2x)^3(y)^1 + 6(2x)^2(y)^2 + 4(2x)^1(y)^3 + 1(2x)^0(y)^4$$

$$16x^4 + 32x^3y + 24x^2y^2 + 8xy^3 + y^4$$

c) $(3x-2y)^5$

$$1(3x)^5(-2y)^0 + 5(3x)^4(-2y)^1 + 10(3x)^3(-2y)^2 + 10(3x)^2(-2y)^3 + 5(3x)^1(-2y)^4 + 1(3x)^0(-2y)^5$$

$$244x^5 - 810x^4y + 1080x^3y^2 - 720x^2y^3 + 240xy^4 - 32y^5$$

2) $(5+2x)^4$

$$4(5)^1(2x)^3$$

a) $160x^3$ coefficient = 160

2b) $(2-3x)^5$

$$10(2)^2(-3x)^3$$

$$-1080x^3$$
 coefficient = -1080

c) $(3 - \frac{1}{2}x)^4$

$$4(3)^1(-\frac{1}{2}x)^3$$

$$-\frac{3}{2}x^3$$
 coefficient = $-\frac{3}{2}$

3) $(1-2x)(1+3x)^3$

$$1(1)^3(3x)^0 + 3(1)^2(3x)^1 + 3(1)^1(3x)^2 + 1(1)^0(3x)^3$$

$$1 + 9x + 27x^2 + 27x^3$$

$$(1 + 9x + 27x^2 + 27x^3)(1 - 2x)$$

$$1 - 2x + 9x - 18x^2 + 27x^2 - 54x^3 + 27x^3 - 54x^4$$

$$1 + 7x + 9x^2 - 27x^3 - 54x^4$$

$$4) (2 + 3x)^4$$

$$1(2)^4(3x)^0 + 4(2)^3(3x)^1 + 6(2)^2(3x)^2 + 4(2)^1(3x)^3 + 1(2)^0(3x)^4$$

$$a) 16 + 96x + 216x^2 + 216x^3 + 81x^4$$

$$b) 16 - 96x + 216x^2 - 216x^3 + 81x^4$$

$$5) \text{ coefficient of } x^2 = 1350$$

$$6 \times (3)^2 \times (xk)^2$$

$$54x^2k^2$$

$$54k^2 = 1350$$

$$54k^2 - 1350$$

$$k^2 - 25 = 0$$

$$(k+5)(k-5) \quad k = \pm 5$$

$$6) (4+k)^3$$

$$1(4)^3(k)^0$$

$$3(4)^2(k)^1$$

$$3(4)^1(k)^2$$

$$1(4)^0(k)^3$$

$$a) 64$$

$$+ 48k$$

$$+ 12k^2$$

$$+ k^3$$

$$b) (4 + x^2 - x)^3$$

$$a = 4$$

$$b = x^2 - x$$

$$n = 3$$

$$1(4^3) + 3(4)^2(x^2-x)^1 + 3(4)^1(x^2-x)^2 + 1(4)^0(x^2-x)^3$$

$$64 + 48x^2 - 48x + 12x^4 - 24x^3 + 12x^2 + x^6 - 3x^5 + 3x^4 - x^3$$

$$64 - 48x + 60x^2 - 25x^3 + 15x^4 - 3x^5 + x^6$$

$$7) (5+x)(2-kx)^3$$

$$3(2)^2(-kx)^1$$

$$3(2)^1(-kx)^2$$

$$-12kx$$

$$+ 6k^2x^2$$

$$(-12kx)(x) \quad (5)(6k^2x^2)$$

$$-12kx^2 + 30k^2x^2$$

$$30k^2 - 12k - 18 = 0$$

$$k = 1 \quad k = -\frac{3}{5}$$

$$\begin{array}{r} -3 \\ / \backslash \\ -3 \quad 1 \end{array}$$