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5 continued -

$$k = -15$$

$$\begin{aligned} & (x-5)(x+3) \\ &= x^2 + 3x - 5x - 15 \\ &= x^2 - 2x - 15 \end{aligned}$$

**EIP** (6)  $\frac{4x^2 + 8x - 5}{6x^2 - 7x + k} = \frac{2x + 5}{3x - 2}$

↓ (factorise)

$$\begin{aligned} & 4x^2 + 8x - 5 \\ &= (2x-1)(2x+5) \end{aligned}$$

$$\frac{(2x-1)(2x+5)}{(3x-2)(2x+5)}$$

both cancelled out to receive given answer

$$\frac{(2x-1)(2x+5)}{(3x-2)(2x+5)} = \frac{(3x-2)(2x+5)}{6x^2 + 15x - 4x - 10}$$

$$(3x-2)(2x-1) \Rightarrow 6x^2 - 3x - 4x + 2 = 6x^2 - 7x + 2$$

$$k = 2$$

**EIP** (7)

$$\frac{6x^3 - 2x^2 - 4x}{2x^2 - 7x + 5}$$

$$\Rightarrow \frac{2x(3x+2)(x-1)}{(2x-5)(x-1)} = \frac{2x(3x+2)}{(2x-5)} = \frac{ax(bx+c)}{px+q}$$

$$a=2, b=3, c=2, p=2, q=-5$$

RF MATHS

Dividing polynomials - 7.2

1) a)

$$\begin{array}{r} 2x^2 + 3x + 5 \\ x-1 \overline{) 2x^3 - 5x^2 + 8x - 5} \\ \underline{2x^3 - 2x^2} \phantom{+ 8x - 5} \\ -3x^2 + 8x \phantom{- 5} \\ \underline{-3x^2 + 3x} \phantom{- 5} \\ 5x - 5 \\ \underline{5x - 5} \\ 0 \end{array}$$

$$(x-1)(2x^2 + 3x + 5)$$

b)

$$\begin{array}{r} 3x^2 + 2x - 7 \\ x+2 \overline{) 3x^3 + 8x^2 + 3x - 2} \\ \underline{3x^3 + 6x^2} \phantom{+ 3x - 2} \\ 2x^2 + 3x \phantom{- 2} \\ \underline{-2x^2 + 4x} \phantom{- 2} \\ 7x - 2 \\ \underline{-7x + 14} \\ 12 \end{array}$$

$$\begin{array}{r} 2x^2 + 3x \\ -2x^2 + 4x \\ \hline -x - 2 \quad (-1x(x+2)) \\ \underline{-x - 2} \\ 0 \end{array}$$

$$\text{Ans} = (3x^2 + 2x - 7)(x+2)$$

c)

$$\begin{array}{r}
 2x^2 + 7x + 4 \\
 \hline
 n-3 \overline{) 2x^3 + x^2 - 17x - 12} \\
 \underline{2x^3 - 6x^2} \phantom{- 17x - 12} \\
 7x^2 - 17x - 12 \\
 \underline{7x^2 - 21x} \phantom{- 12} \\
 4x - 12 \\
 \underline{4x - 12} \\
 0
 \end{array}$$

ANS =  $(2x^2 + 7x + 4)(n-3)$

d)

$$\begin{array}{r}
 4x^2 - 3x + 1 \\
 \hline
 4x \ x + 4 \overline{) 4x^3 + 13x^2 - 11x + 4} \\
 \underline{4x^3 + 16x^2} \phantom{- 11x + 4} \\
 -3x^2 - 11x + 4 \\
 \underline{-3x^2 - 12x} \phantom{+ 4} \\
 x + 4 \\
 \underline{x + 4} \\
 0
 \end{array}$$

ANS =  $(4x^2 - 3x + 1)(n+4)$

2) a)

$$\begin{array}{r}
 3x^3 + 2x^2 - 5x - 3 \\
 \hline
 x+2 \overline{) 3x^4 + 8x^3 - x^2 - 13x - 6} \\
 \underline{3x^4 + 6x^3} \phantom{- x^2 - 13x - 6} \\
 2x^3 - x^2 - 13x - 6 \\
 \underline{2x^3 + 4x^2} \phantom{- 13x - 6} \\
 -5x^2 - 13x - 6 \\
 \underline{-5x^2 - 10x} \phantom{- 6} \\
 -3x - 6 \\
 \underline{-3x - 6} \\
 0
 \end{array}$$

ANSWER =  $(3x^3 + 2x^2 - 5x - 3)$

b)

$$\begin{array}{r}
 2x^3 - 5x^2 + 3x - 2 \\
 \hline
 2x+1 \overline{) 4x^4 - 8x^3 + x^2 - x - 2} \\
 \underline{4x^4 + 2x^3} \phantom{+ x^2 - x - 2} \\
 -10x^3 + x^2 - x - 2 \\
 \underline{-10x^3 - 5x^2} \phantom{- x - 2} \\
 6x^2 - x - 2 \\
 \underline{6x^2 + 3x} \phantom{- 2} \\
 -4x - 2 \\
 \underline{-4x - 2} \\
 0
 \end{array}$$

ANSWER =  $(2x^3 - 5x^2 + 3x - 2)$

c)

~~$$\begin{array}{r}
 9x^4 - 3x^3 - 17x^2 \\
 \hline
 3x-2 \overline{) 9x^4 - 3x^3 - 17x^2 + 13x - 2} \\
 \underline{9x^4 - 6x^3} \phantom{+ 13x - 2} \\
 3x^3 - 17x^2 + 13x - 2 \\
 \underline{3x^3 - 2x^2} \phantom{+ 13x - 2} \\
 -15x^2 + 13x - 2 \\
 \underline{-15x^2 + 10x} \phantom{- 2} \\
 3x - 2 \\
 \underline{3x - 2} \\
 0
 \end{array}$$~~

ANSWER =  $(3x^2 + x^2 - 5x + 1)$

d)

$$\begin{array}{r}
 2x^3 - 3x^2 - 7x - 3 \\
 \hline
 2x-3 \overline{) 4x^4 - 12x^3 - 5x^2 + 15x + 9} \\
 \underline{4x^4 - 6x^3} \phantom{+ 9} \\
 -6x^3 - 5x^2 + 15x + 9 \\
 \underline{-6x^3 + 9x^2} \phantom{+ 9} \\
 -14x^2 + 15x + 9 \\
 \underline{-14x^2 + 21x} \phantom{+ 9} \\
 -6x + 9 \\
 \underline{-6x + 9} \\
 0
 \end{array}$$

Answer =  $(2x^3 - 3x^2 - 7x - 3)$

3a)

$$\begin{array}{r}
 2x^2 + 4x - 4 \\
 \hline
 x+1 \overline{) 2x^3 + 6x^2 + 0x - 4} \\
 \underline{2x^3 + 2x^2} \phantom{+ 0x - 4} \\
 4x^2 + 0x - 4 \\
 \underline{4x^2 + 4x} \phantom{- 4} \\
 -4x - 4 \\
 \underline{-4x - 4} \\
 0
 \end{array}$$

Answer =  $(2x^2 + 4x - 4)$

b)

$$\begin{array}{r}
 3x^2 - 2x + 6 \\
 \hline
 x+3 \overline{) 3x^3 + 7x^2 + 0x + 18} \\
 \underline{3x^3 + 9x^2} \phantom{+ 0x + 18} \\
 -2x^2 + 0x + 18 \\
 \underline{-2x^2 - 6x} \phantom{+ 18} \\
 6x + 18 \\
 \underline{6x + 18} \\
 0
 \end{array}$$

Answer =  $(3x^2 - 2x + 6)$

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c)

$$\begin{array}{r}
 4x^2 + 8x + 5 \\
 \hline
 x-2 \overline{) 4x^3 + 0x^2 - 11x - 10} \\
 \underline{4x^3 - 8x^2} \phantom{- 11x - 10} \\
 8x^2 - 11x - 10 \\
 \underline{8x^2 - 16x} \phantom{- 10} \\
 5x - 10 \\
 \underline{5x - 10} \\
 0
 \end{array}$$

Answer =  $(4x^2 + 8x + 5)$

d)

$$\begin{array}{r}
 2x^2 - 3x + 15 \\
 \hline
 x+5 \overline{) 2x^3 + 7x^2 + 0x + 75} \\
 \underline{2x^3 + 10x^2} \phantom{+ 0x + 75} \\
 -3x^2 + 0x + 75 \\
 \underline{-3x^2 - 15x} \phantom{+ 75} \\
 15x + 75 \\
 \underline{15x + 75} \\
 0
 \end{array}$$

Answer =  $(x+5)(2x^2 - 3x + 15)$

7.2 continued

4)

a)

$$\begin{array}{r}
 x^2 - x + 9 \\
 \hline
 x + 4 \overline{) x^3 + 3x^2 + 5x - 8} \\
 \underline{- x^3 + 4x^2} \phantom{- 8} \\
 \phantom{- x^3 +} -x^2 + 5x \phantom{- 8} \\
 \phantom{- x^3 +} \underline{- -x^2 - 4x} \phantom{- 8} \\
 \phantom{- x^3 +} \phantom{- -x^2 -} 9x - 8 \\
 \phantom{- x^3 +} \phantom{- -x^2 -} \underline{- 9x + 36} \\
 \phantom{- x^3 +} \phantom{- -x^2 -} \phantom{9x -} -44.
 \end{array}$$

remainder = ~~-44.~~

b)

$$\begin{array}{r}
 2x^2 + x + 15 \\
 \hline
 x - 3 \overline{) 2x^3 - 5x^2 + 12x - 20} \\
 \underline{- 2x^3 + 6x^2} \phantom{- 20} \\
 \phantom{- 2x^3 +} x^2 + 12x \phantom{- 20} \\
 \phantom{- 2x^3 +} \underline{- x^2 - 3x} \phantom{- 20} \\
 \phantom{- 2x^3 +} \phantom{- x^2 -} 15x - 20 \\
 \phantom{- 2x^3 +} \phantom{- x^2 -} \underline{- 15x - 45} \\
 \phantom{- 2x^3 +} \phantom{- x^2 -} \phantom{15x -} 25
 \end{array}$$

remainder = 25.

c)

$$\begin{array}{r}
 3x^2 - 13x + 25 \\
 \hline
 x + 5 \overline{) 3x^3 + 2x^2 - 40x + 45} \\
 \underline{- 3x^3 + 15x^2} \phantom{- 40x + 45} \\
 \phantom{- 3x^3 +} -13x^2 - 40x \phantom{+ 45} \\
 \phantom{- 3x^3 +} \underline{- -13x^2 - 65x} \phantom{+ 45} \\
 \phantom{- 3x^3 +} \phantom{- -13x^2 -} 25x + 45 \\
 \phantom{- 3x^3 +} \phantom{- -13x^2 -} \underline{- 25x + 125} \\
 \phantom{- 3x^3 +} \phantom{- -13x^2 -} \phantom{25x +} -80
 \end{array}$$

remainder = ~~-80.~~

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5) E

$$\begin{array}{r}
 -3x^2 + 4x - 1 \\
 \hline
 5x - 2 \overline{) -15x^3 + 26x^2 - 13x + 5} \\
 \underline{- -15x^3 + 6x^2} \phantom{- 13x + 5} \\
 \phantom{- -15x^3 +} 20x^2 - 13x \phantom{+ 5} \\
 \phantom{- -15x^3 +} \underline{- 20x^2 - 8x} \phantom{+ 5} \\
 \phantom{- -15x^3 +} \phantom{- 20x^2 -} -5x + 5 \\
 \phantom{- -15x^3 +} \phantom{- 20x^2 -} \underline{- -5x + 2} \\
 \phantom{- -15x^3 +} \phantom{- 20x^2 -} \phantom{-5x +} 3
 \end{array}$$

remainder = 3.

EIP

6) a)

$$\begin{array}{r}
 6x^2 - 31x + 80 \\
 \hline
 x + 3 \overline{) 6x^3 - 13x^2 - 13x + 30} \\
 \underline{- 6x^3 + 18x^2} \phantom{- 13x + 30} \\
 \phantom{- 6x^3 +} -31x^2 - 13x \phantom{+ 30} \\
 \phantom{- 6x^3 +} \underline{- -31x^2 - 93x} \phantom{+ 30} \\
 \phantom{- 6x^3 +} \phantom{- -31x^2 -} 80x + 30 \\
 \phantom{- 6x^3 +} \phantom{- -31x^2 -} \underline{- 80x + 240} \\
 \phantom{- 6x^3 +} \phantom{- -31x^2 -} \phantom{80x +} -210
 \end{array}$$

remainder = ~~-210.~~

b)

$$\begin{array}{r}
 6x^2 - x - 15 \\
 x-2 \overline{) 6x^3 - 13x^2 - 13x + 30} \\
 \underline{- 6x^3 + 12x^2} \phantom{- 13x + 30} \\
 \phantom{- 6x^3 +} 2x^2 - 13x \phantom{+ 30} \\
 \underline{- 2x^2 + 4x} \phantom{+ 30} \\
 \phantom{- 6x^3 +} \phantom{2x^2 -} -9x + 30 \\
 \underline{- 9x + 18} \\
 \phantom{- 6x^3 +} \phantom{2x^2 -} \phantom{-9x +} 12 \\
 \underline{- 12x + 24} \\
 \phantom{- 6x^3 +} \phantom{2x^2 -} \phantom{-9x +} \phantom{12} 0
 \end{array}$$

$$\begin{aligned}
 & 6x^2 - x - 15 \quad (\text{factorise this}) \\
 & = 6x^2 + 9x - 10x - 15 \\
 & = 3x(2x + 3) - 5(2x + 3) \\
 & = (3x - 5)(2x + 3)
 \end{aligned}$$

EIP

7

a)

$$\begin{array}{r}
 2x^2 + 3x + 5 \\
 x+3 \overline{) 2x^3 + 3x^2 - 4x + k} \\
 \underline{- 2x^3 + 6x^2} \phantom{- 4x + k} \\
 \phantom{- 2x^3 +} -3x^2 - 4x \phantom{+ k} \\
 \underline{- 3x^2 + 9x} \phantom{+ k} \\
 \phantom{- 2x^3 +} \phantom{-3x^2 -} 13x + k \\
 \underline{- 13x + 15} \\
 \phantom{- 2x^3 +} \phantom{-3x^2 -} \phantom{13x +} k - 15
 \end{array}$$

$$\begin{aligned}
 k - 15 &= 0 \\
 k &= 15
 \end{aligned}$$

$$b) f(x) = (x+3)(2x^2 - 3x + 5)$$

$$a) f(x) = 0$$

$$\begin{aligned}
 x + 3 &= 0 \\
 x &= -3
 \end{aligned}$$

one solution

$$\begin{array}{r}
 2x^2 - 3x + 5 \\
 b^2 - 4ac < 0 \\
 a = 2, b = -3, c = 5
 \end{array}$$

$$(-3)^2 - 4(2 \times 5)$$

$$= 9 - 40$$

$$= -31$$

$$-31 < 0$$

no solution

EIP

8

$$\begin{array}{r}
 3x^2 + 16x + 24 \\
 x-2 \overline{) 3x^3 + 10x^2 - 8x - 5} \\
 \underline{- 3x^3 + 6x^2} \phantom{- 8x - 5} \\
 \phantom{- 3x^3 +} 4x^2 - 8x - 5 \\
 \underline{- 4x^2 + 8x} \phantom{- 5} \\
 \phantom{- 3x^3 +} \phantom{4x^2 -} 16x - 5 \\
 \underline{- 16x + 32} \\
 \phantom{- 3x^3 +} \phantom{4x^2 -} \phantom{16x -} 27 \\
 \underline{- 27x + 54} \\
 \phantom{- 3x^3 +} \phantom{4x^2 -} \phantom{16x -} \phantom{27} 0
 \end{array}$$

$$\text{remainder} = 43$$

$$b) f(x) = (x-2)(3x^2 + 16x + 24) + 43$$

a)  $f(x) = 10x^3 - 19x^2 + 4x + 15$

$(x-1)(10x^2 - 19x - 15)$

$$\begin{array}{r}
 10x^2 - 19x - 15 \\
 x-1 \overline{) 10x^3 - 19x^2 + 4x + 15} \\
 \underline{-10x^3 - 10x^2} \phantom{+ 4x + 15} \\
 -19x + 4x \phantom{+ 15} \\
 \underline{-19x + 19x} \phantom{+ 15} \\
 15x + 15 \\
 \underline{-15x + 15} \\
 0
 \end{array}$$

b)  $(x-1)(10x^2 - 19x - 15)$

$$\begin{array}{l}
 10x^2 - 19x - 15 \\
 10x^2 - 25x + 6x - 15 \\
 5x(2x-5) + 3(2x-5) \\
 (5x+3)(2x-5)
 \end{array}$$

Ans -  $(x-1)(5x+3)(2x-5)$

c)  $x-1=0$   
 $x=1$   
 $5x+3=0$   
 $5x=-3$   
 $x=-\frac{3}{5}$

$2x-5=0$   
 $2x=5$   
 $x=\frac{5}{2}$       Ans -  $x=1, -\frac{3}{5}, \frac{5}{2}$

7.3 - The Factor Theorem

(1) a)  $(x+1)$  is a factor of  $2x^3 + 7x^2 - 5$ . (given)

$x+1=0$   
 $x=-1$   
 $2(-1)^3 + 7(-1)^2 - 5 = 0$   
 $f(-1) = 0$       ↳ as  $f(x+1) = 0$  it is a factor.

b)  $x+2=0$   
 $x=-2$   
 $f(-2) = (-2)^3 + 7(-2)^2 + 3(-2) - 2 = 0$   
 $f(-2) = 0$

c)  $x-3=0$   
 $x=3$   
 $f(3) = 0$   
 $2(3)^3 - 3(3)^2 - 7(3) - 6 = 0$

d)  $x-4=0$   
 $x=4$   
 $f(4) = 0$   
 $2(4)^4 - 3(4)^3 - 15(4) - 4 = 0$