

Author: Elizabeth Boansi

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3.1

$$\begin{array}{r} 1. \text{ (a)} \quad 6x + y = 9 \\ + \quad 4x - y = 1 \\ \hline 10x = 20 \\ x = \frac{20}{10} \end{array}$$

$$x = 2$$

sub in $x = 2$

$$6(2) + y = 9$$

$$12 + y = 9$$

$$y = 9 - 12$$

$$y = -3$$

$$x = 2, y = -3$$

$$\begin{array}{r} \text{(c)} \quad 4x - 3y = 2 \quad (\times 5) \\ 5x - 7y = 9 \quad (\times 4) \end{array}$$

$$20x - 15y = 10$$

$$- \quad 20x - 28y = 36$$

$$0 + 13y = -26$$

$$y = \frac{-26}{13}$$

$$y = -2$$

sub in $y = -2$

$$4x - 3(-2) = 2$$

$$4x + 6 = 2$$

$$4x = 2 - 6$$

$$4x = -4$$

$$x = -1$$

$$\begin{array}{r} \text{(b)} \quad 2x + 3y = 8 \quad (\times 1.5) \\ 3x + 2y = 7 \end{array}$$

$$3x + 4.5y = 12$$

$$- \quad 3x + 2y = 7$$

$$0 + 2.5y = 5$$

$$y = \frac{5}{2.5}$$

$$y = 2$$

sub in $y = 2$

$$3x + 2(2) = 7$$

$$3x + 4 = 7$$

$$3x = 3$$

$$x = 1$$

$$x = 1, y = 2$$

2. (a) Rearrange

$$x + 4y = 5$$

$$\rightarrow x = 5 - 4y$$

sub $x = 5 - 4y$ into 2nd equation

$$5(5 - 4y) - 2y = 3$$

$$25 - 20y - 2y = 3$$

$$25 - 22y = 3$$

$$-22y = 3 - 25$$

$$-22y = -22$$

$$y = 1$$

(2.a) sub $y=1$

$$x + 4(1) = 5$$

$$x + 4 = 5$$

$$x = 5 - 4$$

$$x = 1$$

$$2x - 6\left(\frac{5}{3} - \frac{4}{3}x\right) = -5$$

$$2x - 10 + 8x = -5$$

$$10x = 5$$

$$x = \frac{5}{10}$$

$$x = 0.5$$

(b) sub $y = 11 - 2x$

into $2x + 5y = 37$

$$2x + 5(11 - 2x) = 37$$

$$2x + 55 - 10x = 37$$

$$55 - 8x = 37$$

$$-8x = 37 - 55$$

$$-8x = -18$$

$$x = \frac{18}{8}$$

$$\text{sub } x = 2.25$$

$$y = 11 - 2(2.25)$$

$$y = 11 - 4.5$$

$$y = 6.5$$

$$x = 2.25, y = 6.5.$$

sub in $x = 0.5$

$$4(0.5) + 3y = 5$$

$$2 + 3y = 5$$

$$3y = 5 - 2$$

$$y = 1$$

$$x = 0.5, y = 1.$$

3: (a) $3x - 3y + 6 = 0$

$$y + x = 8$$

$$x = 8 - y$$

$$3(8 - y) - 3y + 6 = 0$$

$$24 - 3y - 3y + 6 = 0$$

$$-6y = -30$$

$$y = \frac{-30}{-6}$$

$$y = 5$$

(c) Rearrange $4x + 3y = 5$

$$3y = 5 - 4x$$

$$y = \frac{5 - 4x}{3}$$

$$y = \frac{5}{3} - \frac{4}{3}x$$

↳ sub into 2nd equation

sub in $y = 5$

$$5 + x = 8$$

$$x = 3$$

$$3.(b) \quad 5x - 5 = -2y$$

$$3x - 2y = 4y$$

-

$$5x + 2y = 5(x-2)$$

$$3x - 2y = 2y$$

$$-10x - 4y = -10$$

$$\bar{x} \quad 3x - 4y = 2y$$

$$\hline -13x \quad = -3y$$

$$x = \frac{-3y}{-13}$$

$$x = 3$$

sub in $x=3$

$$3(3) - 2y = 4y$$

$$9 - 2y = 4y$$

$$-2y = 4y$$

$$y = \frac{-20}{4}$$

$$y = -5$$

$$3.(c) \quad \frac{5 - 3(5)}{5} = y$$

$$\frac{5 - 15}{5} = y$$

$$y = -2$$

Exam practice.

$$Q4. \quad x + y = 2$$

$$2y = 18x - 6$$

$$\text{Rearrange: } x + y = 2$$

$$+0: y = 2 - x$$

$$2(2 - x) = 18x - 6$$

$$4 - 2x = 18x - 6$$

$$4 + 6 = 18x + 2x$$

$$10 = 20x$$

$$x = \frac{10}{20}$$

$$x = 0.5 \left(\frac{1}{2}\right)$$

$$(c) \quad 4x - y = 22(x-5)$$

$$3x + 5y = 5$$

$$-20x + 5y = -110$$

$$- \quad 3x + 5y = 5$$

$$\hline -23x \quad = -115$$

$$x = \frac{-115}{-23}$$

$$x = 5$$

sub in $x=5$

$$\text{sub } x = 0.5$$

$$2 - 0.5 = 1.5$$

$$y = 1.5$$

$$5. \quad 3x - y = -5$$

$$0.5y + 2x = 4$$

$$\text{Rearrange: } 3x - y = -5$$

$$y = 3x + 5$$

Q5. Sub $y = 3x + 5$

$$0.5(3x + 5) + 2x = 4$$

$$\frac{3}{2}x + \frac{5}{2} + 2x = 4$$

$$\frac{7}{2}x = 4 - \frac{5}{2}$$

$$x = \frac{3}{2} \div \frac{7}{2}$$

$$x = \frac{3}{7}$$

Sub in $x = \frac{3}{7}$

$$3\left(\frac{3}{7}\right) + 5 = y$$

$$y = \frac{44}{7}$$

6. $6ky + 9x = 12$

$$xy - x = 4.5$$

Sub $x = -1$ to both equations

$$6ky + 9(-1) = 12$$

$$6ky - 9 = 12$$

$$6ky = 12 + 9$$

$$6ky = 21$$

$$xy = \frac{21}{6} = \frac{7}{2}$$

$$xy - (-1) = 4.5$$

$$xy = 4.5 - 1$$

$$xy = \frac{7}{2}$$

7. Nisha. You can rearrange each equation to get the other. So any pair of values will satisfy both equations

e.g if $x = 2$

$$4(2) + 6y = 10$$

$$8 + 6y = 10$$

$$6y = 10 - 8$$

$$6y = 2$$

$$y = \frac{1}{3}$$

$$2(2) = 5 - 3y$$

$$4 = 5 - 3y$$

$$4 - 5 = -3y$$

$$-1 = -3y$$

$$\frac{-1}{-3} = y$$

$$y = \frac{1}{3}$$