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## 1.2: Measuring correlation

- ① a) Approximately 0.7    b) Approximately 0.3    c) Approximately -0.9

② a) The type and strength of linear correlation between  $x$  and  $y$

b)  $r = 0.9783$  (4dp)

③ a)  $r = -0.9355$  (4dp)    b) It has a strong negative correlation. The parts of channel with larger depth have a lower current velocity.

④

$x$ :	0	0.3010	0.4771	0.6021	0.6990	0.7782	0.8451	0.9031	0.9542	
$R$	1	2	3	4	5	6	7	8	9	10
$P$	1137	785	578	561	546	535	524	496	492	459
$y$ :	3.0559	2.8949	2.7619	2.7488	2.7372	2.7284	2.7193	2.6955	2.6919	2.6621

$r = -0.954$  (3sf)

⑤ a)

Population, $P$ (1000s)	87	9	73	62	7	44	53	98	29	35
Waste, $W$ (tonnes 1000s)	95	19	58	41	14	37	47	82	24	26
$\log W$	1.98	1.28	1.76	1.61	1.15	1.57	1.67	1.91	1.38	1.41

b)  $r = 0.975$  (3sf)

c) There is a strong positive linear correlation with data in the form  $\log W$  against  $P$ , which suggests an exponential model is a good fit.

d)  $y = 1.15 + 0.0085x \Rightarrow \log W = 1.15 + 0.0085P \Rightarrow W = 10^{1.15} \times 10^{0.0085P}$

$a = 10^{1.15} = 14.1$      $b = 10^{0.0085} = 1.02$  (3sf)

⑥ a)

Engine size, $E$ (litres)	3.2	3.2	2.8	2.5	2.8	1.8	5	6	2.3	3.5
Fuel economy, $M$ (mpg)	24	26	26	27	26	29	21	19	30	23
$\log E$	0.505	0.505	0.447	0.398	0.447	0.255	0.669	0.778	0.362	0.544
$\log M$	1.38	1.41	1.41	1.43	1.41	1.46	1.32	1.28	1.48	1.36

b)  $r = -0.962$

c) There is a strong negative linear correlation with data in the form  $\log M$  against  $\log E$ , which suggests a model of the form  $y = kx^n$  is a good fit.

a)  $y = 1.59 - 0.383x \Rightarrow \log M = 1.59 - 0.383(\log E) \Rightarrow \log M = 1.59 - 0.383 \log E$   
 $\Rightarrow M = 10^{1.59} \times E^{-0.383} \Rightarrow k = 10^{1.59} = 38.9, n = -0.383$  (3sf)

⑦ a)  $r = -0.852$

b)  $-0.852$  is close to  $-1$ , so the data values show a strong to moderate negative correlation. A linear regression model is suitable for these data.

⑧ a) n/a:  $\rightarrow$  Data on daily maximum gust is not available for this day.

b)  $r = -0.0549$ ; The n/a data entry is omitted when calculating  $r$ .

c) Jamie's statement is not valid because there may be a non-linear relationship between the two variables or the sample size is too small to draw this conclusion.

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