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Solution Bank 6.2

- ① a) Yes - all binomial conditions met
b) No - not a fixed number of trials
c) No - not a fixed probability of success
d) Yes - fixed number of independent trials, 2 possible outcomes and fixed probability of success

③ a) $P(Y=6)$
$$\binom{12}{6} (0.3)^6 (0.7)^6$$
$$= 924 \times 0.000729 \times 0.117649$$
$$= \underline{0.1766}$$

b) $P(Y < 2) = P(0) + P(1)$
 $P(Y < 2) = \underline{0.0639}$

c) $P(Y \geq 9) = 1 - P(Y \leq 8)$
 $= \underline{0.2253}$

- ⑤ a) the lifetimes are independent of each other, there are fixed numbers of trials, and the probability a battery lasts < 30hrs is constant

b) $P(X=3) = \underline{0.2242}$

c) $P(X \leq 2) = \underline{0.5631}$

⑥ a) $P(\text{likes chocolate}) = 0.5$
 $X \sim B(10, 0.5)$

b) i) $P(X=4)$
 $P(X=4) = \underline{0.1348}$

ii) $P(X > 4)$
 $= 1 - P(X \leq 4)$
 $= \underline{0.013}$

② a) $P(X=2) = \binom{6}{2} (0.2)^2 (0.8)^4$
 $= 15 \times 0.04 \times 0.4096$
 $= \underline{0.24576}$

b) $P(1) = \binom{6}{1} (0.2)^1 (0.8)^5 = 6 \times 0.2$
 $\underline{0.01536}$ $= 0.32768$
 $= 0.3432$

c) $0.2621 + 0.3432$
 $= \underline{0.65536}$

- ④ a) 8 independent trials $n=8$

$p = \frac{4}{5} = 0.8$
 $n=8$ $p=0.8$

b) i) $P(X=5)$
 $\binom{8}{5} (0.4)^5 (0.6)^3$
 $= 56 \times 0.01024 \times 0.216$
 $= \underline{0.1468}$

$P(X=3)$
 $= \underline{0.0092}$
 $P(X \geq 7) = P(7) + P(8)$
 $= \underline{0.5033}$

- ⑦ a) Prime numbers $\rightarrow 2, 3, 5$
probability of success $= 3/6 = 0.5$
 $X \sim B(10, 0.5)$

the rolls are independent of each other; the probability of rolling a prime number is constant

b) $P(X=4)$
 $P(X=4) = \underline{0.2051}$

c) $P(\text{success}) = 0.2051$
 $V \sim B(7, 0.2051)$
Find $P(Y=2)$

$$= \binom{7}{2} (0.2051)^2 (1-0.2051)^5$$
$$= 21 \times 0.0420 \times 0.3276$$
$$= \underline{0.2803}$$